## EP Curriculum Map <br> NSW (NESA) Mathematics Stage 3 to 5

## Stage 3

## Representing numbers

Outcomes

Content Descriptors

- Whole numbers: Recognise, represent and order numbers in the millions
- Whole numbers: Apply place value to partition, regroup and rename numbers to 1 billion
- Decimals and percentages: Recognise that the place value system can be extended beyond hundredths
- Decimals and percentages: Compare, order and represent decimals


## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01
- applies an understanding of place value and the role of zero to represent the properties of numbers MA3-RN-01
- compares and orders decimals up to 3 decimal places MA3-RN-02
- determines percentages of quantities, and finds equivalent fractions and decimals for benchmark percentage values MA3-RN-03


## EP Lessons in 1. Represents numbers $A$

Decimals and percentages

- Introduction to Decimals
- Tenths
- Hundredths
- Thousandths and Beyond
- Comparing Decimals

Practice

- Practice: Comparing Decimals
- Practice: Decimal Place Values
- Practice: Hundredths
- Practice: Introduction to Decimals
- Practice: Tenths
- Practice: Thousandths and Beyond

Hands-on Activity: Place Value Codebreaking

- Place Value Codebreaking
- Place Value Codebreaking Student Worksheet
- Place Value Codebreaking Teacher Guide


## Content Descriptors

- Whole numbers: Locate and represent integers on a number line
- Decimals and percentages: Make connections between benchmark fractions, decimals and percentages
- Decimals and percentages: Determine percentage discounts of 10\%, 25\% and 50\%


## EP Lessons in 2. Represents numbers B

1. Whole numbers

- Number Lines
- Positive Integers
- Ordering Positive Integers
- Introduction to Negative Numbers
- Negative Integers
- Negative Numbers on the Number Line
- Ordering Negative Integers

Practice

- Practice: Negative Integers
- Practice: Ordering Negative Integers
- Practice: Ordering Positive Integers
- Practice: Positive Integers


## 2. Decimals and percentages

- Introduction to Percentages
- Using Percentages
- Discounts
- Calculating Percentage Discounts
- Percentages and Money
- Boxing Day Bonanza

Practice

- Practice: Calculating Percentage Discounts
- Practice: Discounts
- Practice: Percentages and Money
- Practice: Percentages and Populations


## Additional resources

## 3. Topic Tests

- Decimals
- Decimals and Percentages
- Discounts
- Percentages


## Additive relations

| Outcomes | A student: <br> - develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01 <br> - selects and applies appropriate strategies to solve addition and subtraction problems MA3-AR-01 |  |
| :---: | :---: | :---: |
| Content Descriptors | EP Lessons in 1. Additive relations $\mathbf{A}$ |  |
| - Apply efficient mental and written strategies to solve addition and subtraction problems <br> - Use estimation and place value understanding to determine the reasonableness of solutions | 1. Addition and subtraction problems <br> - Addition <br> - Subtraction <br> - The Subtraction Algorithm <br> - Applying Addition and Subtraction <br> - Practice <br> - Practice: Addition <br> - Practice: Applying Addition and Subtraction <br> - Practice: Subtraction | 2. Reasonableness of solutions <br> - Introduction to Rounding <br> - Leading Digit Approximation <br> - Rounding Decimal Numbers |
| Content Descriptors | EP Lessons in 2. Additive relations B |  |
| - Choose and use efficient strategies to solve addition and subtraction problems <br> - Applies known strategies to add and subtract decimals | 1. Addition and subtraction problems <br> - Budgeting <br> - Making a Budget <br> - Practice <br> - Practice: Budgeting <br> - Practice: Making a Budget | 2. Add and subtract decimals <br> - Decimal Place Values <br> - Comparing Decimals <br> - Adding Decimals <br> - Applications of Adding Decimals <br> - Subtracting Decimals <br> - Applications of Subtracting Decimals |
| Additional resources |  |  |
| 3. Glossary <br> - Definitions List: Addition and Subtraction <br> - Definitions List: Budgeting <br> - Definitions MCQ: Addition and Subtraction <br> - Definitions MCQ: Budgeting <br> - Spelling List: Addition and Subtraction | 4. Topic Test Budgeting |  |

## Multiplicative relations

## Outcomes

## Content Descriptors

- Determine products and factors
- Use partitioning and place value to multiply 2-, 3- and 4-digit numbers by one-digit numbers
- Select and apply mental and written strategies to multiply 2-and 3-digit numbers by 2-digit numbers
- Represent and solve division problems with whole number remainders
- Select and apply strategies to divide a number with 3 or more digits by a one-digit divisor
- Use estimation and rounding to check the reasonableness of answers to calculations


## Content Descriptors

- Select and apply strategies to solve problems involving multiplication and division with whole numbers
- Multiply and divide decimals by powers of 10
- Use equivalent number sentences involving multiplication and division to find unknown quantities
- Represent and describe number patterns formed by multiples
- Explore the use of brackets and the order of operations to write number sentences


## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01
- selects and applies appropriate strategies to solve multiplication and division problems MA3-MR-01
- constructs and completes number sentences involving multiplicative relations, applying the order of operations to calculations MA3-MR-02


## EP Lessons in 1. Multiplicative relations A

1. Products and factors

- Factors
- Identifying Factors
- Highest Common Factor
- Factor Trees
- Prime Numbers
- Composite Numbers
- Prime \& Composite Numbers Practice
- Practice: Composite Numbers
- Practice: Factor Trees
- Practice: Factors
- Practice: Prime \& Composite Numbers
- Practice: Prime Numbers


## EP Lessons in 2. Multiplicative relations B

1. Solve problems involving multiplication and division

- Applying Multiplication and Division

2. Multiply and divide decimals by powers of 10

- Multiplying Decimals
- Dividing Decimals by Whole Numbers

Practice

- Practice: Dividing Decimals
- Practice: Multiplying Decimals


## 2. Multiplying 2-, 3- and 4-digit numbers

- Multiplication Using Place Value
- Multiplying Big Numbers
- Column Multiplication
- Multiplication Using Rounding and Compensation
- Multiplying Big Numbers

3. Division

- Division in Parts
- Long Division
- Short Division - Without Remainders
- Short Division - With Whole Number Remainders
. Number patterns
- Multiples
- Applications of Multiples
- Identifying Patterns
- Missing Pieces of Patterns
- Continuing Patterns
- Equivalent Number Sentences
- Describing Patterns
- Gaps in Number Sentences
- Patterns Found in Nature (Year 5-10)

|  | Practice <br> - Practice: Continuing Patterns <br> - Practice: Describing Patterns <br> - Practice: Equivalent Number Sentences <br> - Practice: Gaps in Number Sentences <br> - Practice: Identifying Patterns <br> - Practice: Missing Pieces of Patterns | 4. Order of operations <br> - Order of Operations <br> - Preserving Order of Operations |
| :---: | :---: | :---: |
| Additional resources |  |  |
| 3. Glossary <br> - Definitions List: Multiplication and Division <br> - Definitions MCQ: Multiplication and Division <br> - Spelling List: Multiplication and Division | 4. Topic Test <br> - Order of Operations |  |

## Fractions

## Outcomes

## Content Descriptors

- Recognise the role of the number 1 as representing the whole
- Compare and order common unit fractions
- Solve problems involving addition and subtraction of fractions with the same denominator


## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01
- compares and orders fractions with denominators of $2,3,4,5,6,8$ and 10 MA3-RQF-01
- determines $1 / 2,1 / 4,1 / 5$ and $1 / 10$ of measures and quantities MA3-RQF-02

EP Lessons in 1. Representing quantity fractions $A$

- Fractions
- Using Fractions
- Unit Fractions
- Fractions on a Number Line
- Proper and Improper Fractions
- Adding Whole Numbers and Fractions
- Adding Fractions with the Same Denominator
- Subtracting Fractions from One Whole
- Subtracting Fractions with the Same Denominator


## Practice

- Practice: Adding Fractions with the Same Denominator
- Practice: Fractions
- Practice: Fractions on a Number Line
- Practice: Proper and Improper Fractions
- Practice: Subtracting Fractions from One Whole
- Practice: Subtracting Fractions from Whole Numbers
- Practice: Subtracting Fractions with the Same Denominator
- Practice: Unit Fractions


## Content Descriptors

- Recognise that a fraction can represent a division
- Build up to the whole from a given fractional part
- Use equivalence to add and subtract fractional quantities
- Find fractional quantities of whole numbers (halves, quarters, fifths and tenths)


## EP Lessons in 2. Representing quantity fractions B

- Comparing Fractions
- Fraction of a Quantity

Practice

- Practice: Fraction Word Problems
- Simplifying Fractions
- Equivalent Fractions
- Equivalent Fractions \& Simplifying
- Comparing Fractions with the Same Denominator
- Subtracting Fractions from Whole Numbers
- Adding Fractions with Related Denominators
- Subtracting Fractions with Related Denominators
- Fraction Word Problems


## Additional resources

## 3. Glossary

- Definitions List: Fractions and Decimals
- Definitions MCQ: Fractions and Decimals
- Spelling List: Fractions and Decimals


## 4. Topic Tests

- Fractions 1
- Fractions 2


## Geometric measure

## Outcomes

## Content Descriptors

- Position: Explore the Cartesian coordinate system
- Length: Use metres and kilometres for length and distances
- Length: Measure lengths to find perimeters
- Angles: Estimate, measure and compare angles using degrees
- Angles: Use a protractor to measure and identify types of angles


## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01
- locates and describes points on a coordinate plane MA3-GM-01
- selects and uses the appropriate unit and device to measure lengths and distances including perimeters MA3-GM-02
- measures and constructs angles, and identifies the relationships between angles on a straight line and angles at a point MA3-GM-03


## EP Lessons in 1. Geometric measure A

1. Position

- Locations
- Introduction to Cartesian Planes
- Map Projections: A Matter of Perspective (Year


## 5-10)

Practice

- Practice: Cartesian Planes
- Practice: Locations

2. Length

- Units of Measurement
- Unit Prefixes
- Units of Length
- Perimeter
- Finding Perimeters
- Perimeters of Composite Shapes
- Estimating Measurements

Practice

- Practice: Finding Perimeter
- Practice: Perimeter
- Practice: Units of Length


## 3. Angles

- Angles
- Angles in the Real World
- Right Angles
- Other Common Angles
- Types of Angles
- Measuring Acute and Obtuse Angles
- Measuring Reflex Angles
- Estimating the Size of Angles

Practice

- Practice: Angles
- Practice: Angles in the Real World
- Practice: Estimating the Size of Angles
- Practice: Measuring Acute and Obtuse Angles
- Practice: Measuring Reflex Angles
- Practice: Other Common Angles
- Practice: Right Angles
- Practice: Types of Angles


## Content Descriptors

- Position: Use the 4 quadrants of the coordinate plane
- Length: Connect decimal representations to the metric system
- Length: Convert between common metric units of length
- Length: Solve problems involving the comparison of lengths using appropriate units
- Angles: Investigate angles on a straight line and angles at a point
- Angles: Investigate the relationships formed by the intersection of straight lines


## EP Lessons in 2. Geometric measure B

## 1. Position

- Cartesian Planes
- Introduction to Cartesian Coordinates
- Describing Locations with Coordinates
- Describing Locations with Cartesian Planes
- Practice
- Practice: Cartesian Coordinates
- Practice: Describing Locations with Coordinates

2. Length

- Appropriate Units of Length
- Method for Converting Units of Length
- Converting Units of Length
- Comparing Units of Length
- Interpreting Units of Length

Practice

- Practice: Comparing Units of Length
- Practice: Converting Units of Length
- Practice: Interpreting Units of Length
- Practice: Method of Converting Units of Length
- Practice: Units of Length


## 3. Angles

- Common Angles
- Types of Angles
- Measuring Angles
- Angles in Corners
- Angles on Straight Lines
- Angles Around a Point
- Vertically Opposite Angles

Practice

- Practice: Angles around a Point
- Practice: Angles in Corners
- Practice: Angles on Straight Lines
- Practice: Common Angles
- Practice: Measuring Angles
- Practice: Types of Angles
- Practice: Vertically Opposite Angles


## Additional resources

## 3. Glossary

- Definitions List: Angles
- Definitions List: Length
- Definitions MCQ: Angles


## 4. Topic Tests

- Angles 1
- Angles 2
- Position
- Spelling List: Angles
- Spelling List: Length


## Two-dimensional (2D) spatial structure

| Outcomes | A student: <br> - develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01 <br> - investigates and classifies two-dimensional shapes, including triangles and quadrilaterals based on their properties MA3-2DS-01 <br> - selects and uses the appropriate unit to calculate areas, including areas of rectangles MA3-2DS-02 <br> - combines, splits and rearranges shapes to determine the area of parallelograms and triangles MA3-2DS-03 |  |
| :---: | :---: | :---: |
| Content Descriptors | EP Lessons in 1. Two-dimensional spatial structure $A$ |  |
| - 2D shapes: Classify two-dimensional shapes and describe their properties <br> - Area: Use hectares and square kilometres as units of measurement for area | 1. 2 D shapes <br> - 2D Shapes <br> - Regular Polygons <br> - Irregular Polygons <br> - Composite Shapes <br> - Types of Triangles <br> - Quadrilaterals <br> Practice <br> - Practice: 2D Shapes <br> - Practice: Irregular Polygons <br> - Practice: Regular Polygons | 2. Area <br> - Area <br> - Hectares <br> - Area of Rectangles <br> - Area of Rectangles and Squares <br> Practice <br> - Practice: Area <br> - Practice: Area of Rectangles <br> - Practice: Hectares |
| Content Descriptors | EP Lessons in 2. Two-dimensional spatial structure B |  |
| - 2D shapes: Dissect two-dimensional shapes and rearrange them using translations, reflections and rotations <br> - Area: Find the area of composite figures <br> - Area: Calculate the area of a parallelogram using subdivision and rearrangement <br> - Area: Determine the area of a triangle | 1. 2 D shapes <br> - Translation <br> - Reflection <br> - Rotation <br> - Translation on a Grid <br> - Reflection on a Grid <br> - Rotation on a Grid <br> - The Enlargement Transformation | Geoboard Tetris <br> - Geoboard Tetris <br> - Geoboard Tetris Student Worksheet <br> - Geoboard Tetris Teacher Guide <br> - Paper Geoboard Tetris Student Worksheet <br> - Printable Geoboard |


|  | Practice <br> - Practice: Reflection on a Grid <br> - Practice: Rotation on a Grid <br> - Practice: The Enlargement Transformation <br> - Practice: Translation on a Grid <br> 2. Area <br> - Area of Parallelograms <br> - Area of Triangles <br> - Area of Composite Shapes | Practice <br> - Practice: Area of Parallelograms <br> - Practice: Area of Rectangles \& Squares <br> - Practice: Area of Triangles |
| :---: | :---: | :---: |
| Additional resources |  |  |
| 3. Glossary <br> - Definitions List: Two-Dimensional Space <br> - Definitions MCQ: Two-Dimensional Space <br> - Spelling List: Two-Dimensional Space | 4. Topic Tests <br> - Transformations 1 <br> - Transformations 2 <br> - Two-Dimensional Shapes |  |

## Three-dimensional (3D) spatial structure

| Outcomes | A student: <br> - develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01 <br> - visualises, sketches and constructs three-dimensional objects, including prisms and pyramids, making connections to two-dimensional representations MA3-3DS-01 <br> - selects and uses the appropriate unit to estimate, measure and calculate volumes and capacities MA3-3DS-02 |  |
| :---: | :---: | :---: |
| Content Descriptors | EP Lessons in 1. Three-dimensional spatial structure A |  |
| - 3D objects: Compare, describe and name prisms and pyramids <br> - 3D objects: Connect three-dimensional objects with two-dimensional representations <br> - Volume: Choose appropriate units of measurement for capacity <br> - Volume: Use displacement to investigate volumes of irregular solids <br> - Volume: Connect decimal representations to the metric system | 1. 3D objects <br> - 3D Solids <br> - Prisms <br> - Nets of Prisms <br> - Pyramids <br> - Nets of Pyramids <br> - Identifying Faces of Prisms and Pyramids <br> - Pyramids in the Real World <br> Practice <br> - Practice: 3D Solids <br> - Practice: Identifying Faces of Prisms and Pyramids <br> - Practice: Prisms <br> - Practice: Pyramids <br> - Practice: Pyramids in the Real World <br> 2. Volume <br> - Units of Measurement <br> - Unit Prefixes <br> - Units of Capacity <br> - Interpreting Units of Capacity <br> - Application of Converting Units of Capacity <br> - Converting Units of Capacity <br> - Capacity and Volume | Practice <br> - Practice: Applications of Converting Units of Capacity <br> - Practice: Capacity and Volume <br> - Practice: Converting Units of Capacity <br> - Practice: Interpreting Units of Capacity <br> - Practice: Units of Capacity <br> - Practice: Units of Volume |

## Content Descriptors

- 3D objects: Construct prisms and pyramids
- Volume: Use cubic metres for measurement of volume
- Volume: Recognise the multiplicative structure for finding volume
- Volume: Find the volumes of rectangular prisms in cubic centimetres and cubic metres


## EP Lessons in 2. Three-dimensional spatial structure B

1. 3D objects

Constructing with 3D Objects

- Constructing 3D Objects
- Making Objects Using Cubes
- Making Obiects Using Nets

Playdough Prisms

- Playdough Prisms
- Playdough Prisms Student Worksheet
- Playdough Prisms Teacher Guide
- Playdough Recipe

2. Volume

- Types of Prisms
- Rectangular Prisms
- Volume
- Calculating Volume of Rectangular Prisms Practice
- Practice: Types of Prisms
- Practice: Volume of Rectangular Prisms


## Additional resources

## 3. Glossary

- Definitions List: Volume and Capacity
- Definitions MCQ: Volume and Capacity
- MCQ: Three-Dimensional Space
- Spelling List: Volume and Capacity
- Spelling: Three-Dimensional Space
- Three-Dimensional Space Spelling


## 4. Topic Tests

- Solids 1
- Solids 2


## Non-spatial measure

| Outcomes | A student: <br> - develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01 <br> - selects and uses the appropriate unit and device to measure the masses of objects MA3-NSM-01 <br> - measures and compares duration, using 12- and 24-hour time and am and pm notation MA3-NSM-02 |  |
| :---: | :---: | :---: |
| Content Descriptors | EP Lessons in 1. Non-spatial measure A |  |
| - Mass: Choose appropriate units of measurement for mass <br> - Mass: Connect decimal representations to the metric system <br> - Time: Compare 12- and 24-hour time systems and convert between them | 1. Mass <br> - Units of Measurement <br> - Unit Prefixes <br> - Units of Mass <br> Practice <br> - Practice: Units of Mass <br> 2. Time <br> - Duration <br> - Recording Time <br> - Digital Clocks <br> - 24-Hour Time <br> - Converting 12- and 24-Hour Time <br> - Reading Analog Clocks Basics <br> - Analog Clocks to the Nearest Minute <br> - Timetables <br> - Reading Timetables | Practice <br> - Practice: 24 -Hour Time <br> - Practice: Analog Clocks to the Nearest Minute <br> - Practice: Converting 12- and 24-Hour Time <br> - Practice: Digital Clocks <br> - Practice: Duration <br> - Practice: Reading Analog Clocks Basics <br> - Practice: Reading Timetables <br> - Practice: Recording Time |
| Content Descriptors | EP Lessons in 2. Non-spatial measure B |  |
| - Mass: Convert between common metric units of mass <br> - Time: Solve problems involving duration, using 12- and 24-hour time | 1. Mass <br> - Interpreting Units of Mass <br> - Converting Units of Mass <br> - Net Mass and Gross Mass | Practice <br> - Practice: Applications of Converting Units of Mass <br> - Practice: Converting Units of Mass <br> - Practice: Interpreting Units of Mass <br> - Practice: Net Mass and Gross Mass |


|  | 2. Time <br> - Adding Units of Time <br> - Formatting Time <br> - Personal Timetables <br> - Timetables and Transport | Practice <br> - Practice: Personal Timetables <br> - Practice: Timetables and Transport |
| :---: | :---: | :---: |
| Additional resources |  |  |
| 3. Glossary <br> - Definitions List: Mass <br> - Definitions List: Time <br> - Definitions MCQ: Mass | - Definitions MCQ: Time <br> - Spelling List: Mass <br> - Spelling List: Time | 4. Topic Tests <br> - Clocks <br> - Timetables and Timelines |

## Data

## Outcomes

## Content Descriptors

- Collect categorical and discrete numerical data by observation or survey
- Choose and use appropriate tables and graphs
- Describe and interpret different datasets in context


## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01
- constructs graphs using many-to-one scales MA3-DATA-01
- interprets data displays, including timelines and line graphs MA3-DATA-02

EP Lessons in 1. Data A

- What is Data?
- Collecting Data
- Surveys
- Data Tables
- Tally Marks
- Picture Graphs
- Picture Graphs with Keys
- Picture Graphs and Data Tables


## Practice

- Practice: Collecting Data
- Practice: Data Tables
- Practice: Dot Plots
- Practice: Dot Plots and Tables
- Practice: Picture Graphs
- Practice: Picture Graphs and Data Tables
- Practice: Picture Graphs with Keys
- Practice: Surveys
- Practice: Tally Marks
- Practice: What is Data


## Content Descriptors

- Interpret and compare a range of data displays
- Interpret data presented in digital media and elsewhere


## EP Lessons in 2. Data B

- Picture Graphs
- Picture Graphs with Keys
- Dot Plots
- Pie Charts
- Column (Bar) Graphs
- Reading Column (Bar) Graphs
- Side-by-Side Column Graphs
- Line Graphs
- Two-Way Tables
- Misleading Data and Graphs


## Practice

- Practice: Column (Bar) Graphs
- Practice: Dot Plots
- Practice: Line Graphs
- Practice: Misleading Data and Graphs
- Practice: Picture Graphs
- Practice: Picture Graphs with Keys
- Practice: Pie Charts
- Practice: Reading Column (Bar) Graphs
- Practice: Side-by-Side Column Graphs
- Practice: Two-Way Tables

Additional resources
3. Glossary

- Definitions List: Data
- Definitions MCQ: Data
- Spelling List: Data

4. Topic Tests

- Data 1
- Data 2


## Chance

| Outcomes | A student: <br> - develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01 <br> - conducts chance experiments and quantifies the probability MA3-CHAN-01 |  |
| :---: | :---: | :---: |
| Content Descriptors | EP Lessons in 1. Chance $A$ |  |
| - List outcomes of chance experiments involving equally likely outcomes and represent probabilities | - The Likelihood Scale <br> - Likelihood of Events <br> - Probability as a Fraction <br> - Equal and Unequal Outcomes <br> - The Probability of Outcomes | Practice <br> - Practice: Chance Games <br> - Practice: Equal and Unequal Outcomes <br> - Practice: Likelihood of Events <br> - Practice: Probability as a Fraction <br> - Practice: The Likelihood Scale <br> - Practice: The Probability of Outcomes |
| Content Descriptors | EP Lessons in 2. Chance $B$ |  |
| - Compare observed frequencies of outcomes with expected results <br> - Create random generators and describe probabilities using fractions <br> - Conduct chance experiments with both small and large numbers of trials | - Writing Probabilities <br> - Proportional Reasoning <br> - Probability Experiments <br> - Observed Outcomes vs. Expected Outcomes <br> - Chance Games <br> - Chance Games from Other Cultures | Practice <br> - Practice: Observed Outcomes vs. Expected Outcomes <br> - Practice: Probability Experiments <br> - Practice: Proportional Reasoning <br> - Practice: Writing Probabilities |
| Additional resources |  |  |
| 3. Glossary <br> - Definitions List: Chance <br> - Definitions MCQ: Chance <br> - Spelling List: Chance | 4. Topic Tests <br> - Chance 1 <br> - Chance 2 |  |

## Prior Learning

- Addition
- Angles: Amount of Turn
- Area
- Area Models for Multiplication
- Collecting Data
- Comparing Lengths and Objects
- Comparing Shapes
- Counting
- Describing Locations
- Differences in Results
- Directional Language
- Expanding Numbers
- Half
- How Likely?
- Impossible and Certain Events
- Language of Time
- Money
- Multi Digit Odd and Even Numbers
- Multiplication
- Number Lines
- Numbers in Written Form
- Odd and Even Numbers
- Patterns with Objects
- Quarters and Eighths
- Reading from Data Displays
- Rectangles
- Rectangles
- Skip Counting Down
- Skip Counting Up
- Splitting Up Time
- Subtracting with Number Lines
- Subtraction
- Subtraction
- The Metric System
- Transforming Shapes
- Triangles
- Units of Measurement


## Stage 4

## Computation with integers

| Outcomes | A student: <br> - develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01 <br> - compares, orders and calculates with integers to solve problems MA4-INT-C-01 |  |
| :---: | :---: | :---: |
| Content Descriptors | EP Lessons in 1. Computation with integers |  |
| - Compare and order integers <br> - Add and subtract positive and negative integers <br> - Multiply and divide positive and negative integers <br> - Apply the 4 operations to integers | 1. Compare and Order Integers <br> - Positive Integers <br> - Negative Integers <br> - Rational Numbers on the Number Line <br> - Comparing \& Ordering Integers <br> Practice <br> - Comparing \& Ordering Integers Practice <br> - Integers Practice <br> 2. Add and subtract positive and negative integers <br> - Addition <br> - Subtraction <br> - Adding Negative Numbers <br> - Negative Integer Addition and Subtraction <br> - Subtracting Negative Numbers <br> - Adding and Subtracting Decimals on a Number Line <br> Practice <br> - Adding \& Subtracting Integers Practice | 3. Multiply and divide positive and negative integers <br> - Multiplication <br> - Division <br> - Long Division <br> - Negative Integer Multiplication and Division <br> - Multiplying Decimals <br> - Dividing Decimals <br> 4. Apply the 4 operations to integers <br> - Order of Operations <br> Practice <br> - Order of Operations 1 <br> - Order of Operations 2 <br> - Order of Operations 3 <br> 5. Glossary <br> - Definitions List: Computation with Integers <br> - Definitions MCQ: Computation with Integers |

## Fractions, decimals and percentages

## Outcomes

## Content Descriptors

- Compare fractions using equivalence
- Round decimals to a specified degree of accuracy using approximations
- Identify terminating and recurring decimals
- Identify and make use of the relationship between fractions, decimals and percentages to carry out simple conversions
- Examine the concept of irrational numbers
- Order and compare the value of fractions, decimals and percentages
- Solve problems that involve the addition and subtraction of fractions
- Solve problems that involve the multiplication and division of fractions and decimals
- Represent one quantity as a fraction, decimal or percentage of another, with and without the use of digital tools
- Solve problems that involve the use of percentages


## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01
- represents and operates with fractions, decimals and percentages to solve problems MA4-FRC-C-01


## EP Lessons in 2. Fractions, decimals and percentages

## 1. Fractions

1. Comparing Fractions

- Equivalent Fractions
- Mixed Numbers
- Fraction Walls
- Improper Fractions
- Fractions and Number Lines
- Comparing Fractions
- Comparing Fractions with the Same Denominator
- Simplifying Fractions

Practice

- Practice: Comparing Fractions as Decimals
- Practice: Comparing Fractions with the Same Denominator

2. Adding and Subtracting Fractions

- Adding Fractions with the Same Denominator
- Subtracting Fractions with the Same Denominator
- Adding Fractions with a Different Denominator
- Subtracting Fractions with a Different Denominator
- Adding Mixed Fractions with the Same Denominator
- Subtracting Mixed Fractions with the Same Denominator
- Subtracting Mixed Fractions with a Different Denominator

Practice

- Practice: Adding Fractions with a Different Denominator
- Practice: Adding Fractions with the Same Denominator
- Practice: Subtracting Fractions with a Different Denominator
- Practice: Subtracting Fractions with the Same Denominator
- Practice: Subtracting Mixed Numbers with a Different Denominator

3. Multiplying and Dividing Fractions

- Multiplying Fractions Numerically
- Multiplying Fractions Using Models
- Dividing Fractions
- Dividing Fractions by Simplifying

Practice

- Practice: Dividing Fractions
- Practice: Multiplying Fractions

4. Using Fractions

- Using Fractions in Context
- Using Fractions - Food
- Using Fractions - Space
- Using Fractions - Money

Practice

- Practice: Fractions and Food
- Practice: Fractions and Shopping
- Practice: Fractions and the Cosmos


## 2. Decimals

- How Decimals Work
- Recurring Decimals
- Rounding to Decimal Places
- Terminating Decimals and Rounding
- Multiplying Decimals
- Dividing Decimals

3. Percentages

- Introduction to Percentages
- Using Percentages
- Discounts
- Calculating Discounts
- Calculating Percentage Discounts
- Percentages and Money
- Percentages and Populations
- Profit and Loss
- Calculating Profit and Loss
- Supply Chains
- Goods and Services Tax
- Income Tax
- Maths in Context: Boxing Day Bonanza

Practice

- Practice: Calculating Discounts
- Practice: Calculating Percentage Discounts
- Practice: Calculating Profit and Loss
- Practice: Discounts
- Practice: Percentages and Money
- Practice: Profit and Loss
- Practice: Supply Chains
- Uses of Financial Mathematics Practice

4. Converting Between Real Numbers

- Converting Between Fractions and Decimals
- Converting Between Percentages and Fractions: Simplifying Fractions
- Application: Town Planning

Hands-On Activity: Real Number Dominoes

- Real Number Dominoes
- Real Number Dominoes Student Worksheet
- Real Number Dominoes Teacher Guide

Practice

- Practice: Converting Between Decimals and Percentages
- Practice: Converting Between Fractions and Decimals
- Practice: Converting Between Percentages and Fractions


## 5. Irrational Numbers

- Irrational Numbers
- Happy Pi Day!

Practice

- Practice: Irrational Numbers

6. Glossary

- Definitions List: Decimals
- Definitions List: Finance
- Definitions List: Fractions
- Definitions List: Irrational Numbers
- Definitions List: Money and Financial Mathematics
- Definitions List: Percentages
- Definitions List: Percentages
- Definitions List: Real Numbers
- Definitions MCQ: Decimals
- Definitions MCQ: Finance
- Definitions MCQ: Fractions
- Definitions MCQ: Irrational Numbers
- Definitions MCQ: Money and Financial Mathematics
- Definitions MCQ: Percentages
- Definitions MCQ: Percentages
- Definitions MCQ: Real Numbers
- Spelling List: Money and Financial Mathematics

|  |  | - Discounts and GST |
| :--- | :--- | :--- |
|  | - Eractions, Decimals and Percentages |  |

## Ratios and rates

## Outcomes

## Content Descriptors

- Recognise and simplify ratios
- Solve problems involving ratios
- Recognise and simplify rates
- Solve problems involving rates
- Interpret and construct distance-time graphs from authentic data


## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01
- solves problems involving ratios and rates, and analyses distance-time graphs MA4-RAT-C-01


## EP Lessons in 3. Ratios and rates

## 1. Ratios

- Ratios Introduction
- Ratios
- Maps and Scales

Hands-On Activity: Planning a Party

- Planning a Party
- Planning a Party Student Worksheet
- Planning a Party Teacher Guide

Practice

- Practice: Ratios
- Practice: Ratios II

2. Rates

- Rates
- Applying Ratios and Rates
- Cost per Item
- Best Buys Using Unit Costs
- When a Best Buy isn't the Best Option
- Budgeting: Preparing a Personal Budget
- Water Evaporation Graphs
- Extension: Solving Practical Measurement Problems


## Practice

- Calculating a Best Buy Practice
- Cost per Item Practice
- Mixed Practice: Ratios and Rates
- Practice: Applying Rates and Ratios
- Practice: Rates
- Unit Pricing Practice

3. Distance-time graphs

- Plotting and Reading Travel Graphs
- Analysing Travel Graphs

4. Glossary

- Definitions List: Ratios and Rates
- Definitions MCQ: Ratios and Rates

5. Topic Test

- Rates and Ratios


## Algebraic techniques

## Outcomes

## Content Descriptors

- Examine the concept of pronumerals as a way of representing numbers
- Create algebraic expressions and evaluate them by substitution
- Extend and apply the laws and properties of arithmetic to algebraic terms and expressions
- Extend and apply the distributive law to the expansion of algebraic expressions
- Factorise algebraic expressions by identifying numerical and algebraic factors


## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01
- generalises number properties to operate with algebraic expressions including expansion and factorisation MA4-ALG-C-01


## EP Lessons in 4. Algebraic techniques

1. Introduction to Algebra

- Welcome to Algebra
- Order of Operations in Algebra
- Order of Operations in Algebraic Equations
- Translating Between Word Descriptions and Algebraic Expressions
- Translating Between Authentic Situations and Algebraic Expressions
Practice
- Practice: Introduction to Algebra
- Practice: Relating Words to Algebra

2. Algebraic Expressions

- Substitution
- Arithmetic in Algebra
- Substitution in Algebraic Expressions
- Using Formulas
- Finding Formulas
- Writing and Evaluating Algebraic Expressions
- Translating Between Situations and Algebraic Expressions
Practice
- Practice: Arithmetic Laws and Algebra
- Practice: Formulas
- Practice: Translating Between Situations and Algebraic Expressions
- Practice: Writing and Evaluating Algebraic Expressions


## 3. Simplifying and Evaluating Algebra

- Simplifying Addition in Algebra
- Simplifying Subtraction in Algebra
- Simplifying Multiplication in Algebra
- Simplifying Division in Algebra
- Evaluating Algebraic Expressions
- Simplifying Addition and Subtraction
- Simplifying Multiplication and Division
- The Commutative Law
- The Associative Law

Practice

- Mixed Practice: Patterns and Algebra
- Practice: Associative Law
- Practice: Commutative Law
- Practice: Evaluating Algebraic Expressions
- Practice: Simplifying Addition and Subtraction
- Practice: Simplifying Algebraic Expressions
- Practice: Simplifying Multiplication and Division

4. Distributive Law

- The Distributive Law
- Using the Distributive Law
- Expanding I
- Expanding II


## Practice

- Practice: Distributive Law
- Practice: Expanding I
- Practice: Expanding with Binomial Brackets
- Practice: Expanding with Powers
- Practice: Expanding with the Distributive Law

5. Factorising Algebraic Expressions

- Greatest Common Divisor (Highest Common Factor)
- Introduction to Factorising
- Factorising Algebraic Expressions
- Factorising Algebraic Expressions with Powers

Practice

- Practice: Factorising Algebraic Expressions
- Practice: Factorising Algebraic Expressions with Powers
- Practice: Greatest Common Divisor (Highest Common Factor
- Practice: Introduction to Factorising

6. Glossary

- Definitions List: Algebraic techniques
- Definitions MCQ: Algebraic techniques

7. Topic Tests

- Algebraic Techniques
- Arithmetic Laws


## Indices

## Outcomes

## Content Descriptors

- Apply index notation to represent whole numbers as products of powers of prime numbers
- Examine cube roots and square roots
- Use index notation to establish the index laws with positive-integer indices and the zero index


## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01
- operates with primes and roots, positive-integer and zero indices involving numerical bases and establishes the relevant index laws MA4-IND-C-01


## EP Lessons in 5. Indices

## 1. Index Notation

- Index Notation
- Prime Factors and the HCF
- Prime Factors and the LCM
- Applying Prime Factors

Practice

- Mixed Practice: Prime Numbers and Prime Factors
- Practice: Index Notation
- Practice: Prime Factors

2. Cube Roots and Square Roots

- Perfect Squares
- Square Roots
- Square Roots of Non-Perfect Squares
- Fractional Indices

Practice

- Mixed Practice: Squares and Square Roots
- Practice: Fractional Indices
- Practice: Perfect Squares
- Practice: Square Roots
- Practice: Square Roots of Non-Perfect Squares


## 3. The Index Laws and Zero Index

- Multiplying Indices
- Dividing Indices
- The Power of Zero
- Powers of Powers

Practice

- Mixed Practice: Indices
- Practice: Dividing Indices
- Practice: Multiplying Indices
- Practice: Power of Powers
- Practice: The Power of Zero

4. Glossary

- Definitions List: Indices
- Definitions MCQ: Indices

5. Topic Test

- Multiplying and Dividing Indices


## Equations

## Outcomes

## Content Descriptors

- Solve linear equations up to 2 steps
- Solve and verify linear equations by substitution
- Solve quadratic equations


## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01
- solves linear equations of up to 2 steps and quadratic equations of the form 『ax』^2=c MA4-EQU-C-01


## EP Lessons in 6. Equations

## 1. Introduction to Equations

- Using Formulas
- Rearranging and Solving Equations from Formulas
Hands- On Activity: Physically Balancing Equations
- Physically Balancing Equations
- Physically Balancing Equations Student Worksheet
- Physically Balancing Equations Teacher Guide

Practice

- Practice: Solving Equations
- Practice: Using Formulas

2. Solving Linear Equations

- Linear Equations
- Rearranging Linear Equations
- Balancing Equations
- Concrete Models
- Flow Charts
- Visual Methods for Solving Linear Equations
- Solving One-Step Linear Equations
- Solving Two-Step Linear Equations
- Solving Linear Equations with Brackets
- Applications of Linear Equations
- Non-Integer Solutions to Linear Equations
- Checking Solutions
- Problem-Solving: Opening a New Aquarium


## Practice

- Mixed Practice: Methods for Solving Equations
- Practice: Solving Linear Equations with Algebraic Methods
- Practice: Solving Linear Equations with Visual Methods

3. Solving Quadratic Equations

- Solving Simple Quadratic Equations

4. Glossary

- Definitions List: Equations
- Definitions MCQ: Equations
- Spelling List: Equations

5. Topic Test

- Solving Linear Equations


## Length

## Outcomes

## Content Descriptors

- Solve problems involving the perimeter of various quadrilaterals and simple composite figures
- Describe the relationships between the features of circles


## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01
- applies knowledge of the perimeter of plane shapes and the circumference of circles to solve problems MA4-LEN-C-01


## EP Lessons in 8. Length

1. Perimeter

- Perimeter
- Perimeter of Composite Shapes
- Finding the Unknown Side of a Composite Shape
- Calculating the Perimeter of a Shape with an Unknown Side
- Perimeters of Kites, Rhombuses, Trapeziums and Parallelograms
- Perimeter and Circumference of Composite Shapes
Practice
- Practice: Perimeter
- Practice: Perimeter of Composite Shapes

2. Circles

- Parts of a Circle
- Circumference of Circles
- Using the Circumference of Circles
- Constructing Circles

3. Glossary

- Definitions List: Length
- Definitions MCQ: Length
- Spelling List: Length

4. Topic Test

- Perimeter


## Pythagoras and trigonometry

## Outcomes

## Content Descriptors

- Identify and define Pythagoras' theorem
- Examine problems involving Pythagoras' theorem

A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01
- applies Pythagoras' theorem to solve problems in various contexts MA4-PYT-C-01


## EP Lessons in 9. Pythagoras and trigonometry

1. Right-angled triangles (Pythagoras' theorem)

- Parts of a Triangle and the Hypotenuse
- Pythagoras' Theorem

2. Glossary

- Definitions List: Pythagoras and Trigonometry
- Definitions MCQ: Pythagoras and Irrational Numbers

3. Topic Test

- Pythagoras' Theorem


## Area and surface area

## Outcomes

## Content Descriptors

- Develop and use formulas to find the area of rectangles, triangles and parallelograms to solve problems
- Develop and use the formula to find the area of circles and sectors to solve problems
- Develop and use the formulas to find the area of trapeziums, rhombuses and kites to solve problems
- Choose appropriate units of measurement for area and convert between units


## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01
- applies knowledge of area and composite area involving triangles, quadrilaterals and circles to solve problems MA4-ARE-C-01


## EP Lessons in 10. Area and surface area

1. Units of Area

- Units of Area
- Converting Between Units of Area
- Converting Between Units of Area Applications Practice
- Practice: Converting between Units of Area
- Practice: Converting between Units of Area Applications
- Practice: Units of Area

2. Calculating Area

- Area of Rectangles and Squares
- Area of Triangles
- Area of Parallelograms
- Area of Circles
- Using the Area of Circles
- Area of Trapeziums
- Area of Rhombus and Kites
- Area of Composite Shapes

Practice

- Mixed Practice: Area
- Practice: Area of Composite Shapes
- Practice: Area of Parallelograms
- Practice: Area of Parallelograms
- Practice: Area of Rectangles \& Squares
- Practice: Area of Rhombus and Kites
- Practice: Area of Trapeziums
- Practice: Area of Triangles


## 3. Glossary

- Definitions List: Area
- Definitions MCQ: Area
- Spelling List: Area

4. Topic Tests

- Units of Area


## Volume

## Outcomes

## Content Descriptors

- Describe the different views of prisms and solids that have been formed from prism combinations
- Develop and apply the formula to find the volume of a prism to solve problems
- Develop the formula for finding the volume of Practic
a cylinder and apply the formula to solve problems
- Choose appropriate units of measurement for volume and capacity and convert between units


## Angle relationships

## Outcomes

## Content Descriptors

- Apply the language, notation and conventions of geometry
- Identify geometrical properties of angles at a point
- Identify and describe corresponding. alternate and co-interior angles when 2 straight lines are crossed by a transversal, including parallel lines
- Solve numerical problems involving angles using reasoning


## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01
- applies angle relationships to solve problems, including those related to transversals on sets of parallel lines MA4-ANG-C-01


## EP Lessons in 12. Angle relationships

1. Angles

- Language, Notation and Conventions of Geometry
- Parallel Lines
- Angles around Parallel Lines
- Angles in Corners
- Angles around a Point
- Angles on Straight Lines
- Angles Around a Point
- Vertically Opposite Angles
- Geometric Reasoning

Practice

- Angles around a Point Practice
- Angles in Corners Practice
- Angles on Straight Lines Practice
- Mixed Practice: Angle Relationships
- Practice: Angles Around Parallel Lines
- Practice: Angles Around a Point
- Vertically Opposite Angles Practice

2. Glossary

- Definitions List: Angle Relationships
- Definitions MCQ: Angle Relationships
- Spelling List: Angle Relationships

3. Topic Tests

- Angle Relationships
- Angle Relationships


## Properties of geometrical figures

Outcomes

## Content Descriptors

- Classify triangles according to their side and angle properties
- Classify quadrilaterals and describe their properties
- Apply the properties of triangles and quadrilaterals

A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01
- identifies and applies the properties of triangles and quadrilaterals to solve problems MA4-GEO-C-01

EP Lessons in 13. Properties of geometrical figures

1. Triangles

- Types of Triangles
- Angles in a Triangle
- Angles and Triangles
- Interior and Exterior Angles of Triangles

Practice

- Mixed Practice: Triangles
- Practice: Angles in a Triangle
- Practice: Types of Triangles

Triangles in the Real World

- Triangles in the Real World
- Triangles in the Real World Student Worksheet
- Triangles in the Real World Teacher Guide

2. Quadrilaterals

- Classifying Quadrilaterals
- Angles in Quadrilaterals
- Applying Rules to Quadrilaterals
- Classification of Triangles and Quadrilaterals
- Exterior Angles in Triangles and Ouadrilaterals

Practice

- Mixed Practice: Quadrilaterals
- Practice: Angles in a Quadrilateral
- Practice: Types of Quadrilaterals

3. Glossary

- Definitions List: Geometric Reasoning
- Definitions List: Properties of Geometric Figures
- Definitions MCQ: Geometric Reasoning
- Definitions MCQ: Properties of Geometric Figures
- Spelling List: Properties of Geometrical Figures


## Data classification and visualisation

Outcomes

## Content Descriptors

- Classify data as either numerical (discrete or continuous) or categorical (nominal or ordinal) variables
- Display data using graphical representations relevant to the purpose of the data
- Interpret data in graphical representations

A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01
- classifies and displays data using a variety of graphical representations MA4-DAT-C-01


## EP Lessons in 14. Data classification and visualisation

## 1. Displaying Data

- Displaying Data
- Dot Plots and Column (Bar) Graphs
- Line Graphs
- Introduction to Stem and Leaf Plots
- Pie Charts and Divided Bar Graphs
- Histograms
- Frequency Polygons
- Dot Plots
- Stem and Leaf Plots
- Back-to-Back Stem and Leaf Plots
- Selecting Appropriate Graphs
- Creating an Infographic

Lolly Graphs

- Lolly Graphs
- Lolly Graphs Student Worksheet
- Lolly Graphs Teacher Guide

Practice

- Mixed Practice: Displaying Data
- Practice: Back-to-Back Stem and Leaf Plots
- Practice: Displaying Data
- Practice: Dot Plots and Column Graphs
- Practice: Finding Measures of Centre and Spread in Data Displays
- Practice: Histograms
- Practice: Line Graphs
- Practice: Pick Your Display Method
- Practice: Pie Charts and Divided Bar Graphs
- Practice: Stem and Leaf Plots

2. Glossary

- Definitions List: Data classification and visualisation
- Definitions MCQ: Data classification and visualisation
- Spelling List: Data classification and visualisation

3. Topic Test

- Data Displays
- Data Sources and Statistical Reports


## Data analysis

## Outcomes

## Content Descriptors

- Calculate and compare the mean, median, mode and range for simple datasets
- Interpret the effect individual data points have on measures of centre and range
- Analyse datasets presented in various ways and draw conclusions


## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01
- analyses simple datasets using measures of centre, range and shape of the data MA4-DAT-C-02


## EP Lessons in 15. Data analysis

1. Mean, Median, Mode and Range

- Analysing Numerical Data
- Mean
- Median
- Mode
- Comparing Measures of Centre
- The Range
- Calculating Measures of Centre and Spread

Practice

- Mixed Practice: Introduction to Data
- Mixed Practice: Mean, Median and Mode
- Mixed Practice: Shape and Spread in Data
- Practice: Calculating Measures of Centre and Spread
- Practice: Comparing Measures of Centre
- Practice: Introduction to Data
- Practice: Measures of Centre in Grouped Data
- Practice: The Median
- Practice: The Mean
- Practice: The Mode
- Practice: The Range
- Practice: Shape and Mode

2. The Effect of Individual Data Points

- Outliers
- Clusters and Outliers
- Effect of Shape on Mean and Median
- Scrambled Statistics
- Adding and Removing Data
- Samples and Populations
- Implications and Consequences of Big Data

Practice

- Practice: Clusters and Outliers
- Practice: Effect of Shape on Mean and Median
- Practice: Outliers
- Practice: Samples and Populations
- Practice: Symmetry and Skew in Data

3. Analyse Datasets and Draw Conclusions

- Reporting on Statistical Investigations
- Evaluating Statistical Reports and Claims: Data Collection
- Evaluating Statistical Reports and Claims: Data Reporting
- Evaluating Statistical Graphs: Making our Graph
- Evaluating Statistical Graphs: the Shape of the Graph
- Random Sampling


## Practice

- Mixed Practice: Introduction to Data Methods
- Practice: Evaluating Statistical Graphs: Making our Graph
- Practice: Evaluating Statistical Reports and Claims: Data Collection
- Practice: Evaluating Statistical Reports and Claims: Data Reporting
- Practice: Introduction to Data Collection
- Practice: Shape of the Graph

3. Glossary

- Definitions List: Single Variable Data Analysis
- Definitions List: Single Variable Data Analysis
- Definitions MCQ: Single Variable Data Analysis
- Definitions MCQ: Single Variable Data Analysis
- Spelling List: Single Variable Data Analysis

4. Topic Test

- Analysing and Comparing Data
- Investigating and Analysing Data
- Mean. Median, Mode and Range


## Probability

## Outcomes

## Content Descriptors

- Determine probabilities for chance experiments
- Determine probabilities for complementary events


## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01
- solves problems involving the probabilities of simple chance experiments MA4-PRO-C-01


## EP Lessons in 16. Probability

1. Introduction to Probability

- Probability Terminology
- Introduction to Likelihood
- Probability
- What are Events?
- Experimental Probability
- Impossible and Certain Events

Practice

- Mixed Practice: Introduction to Probability
- Practice: Introduction to Probability

2. Exploring Probabilities

- Comparing Probabilities
- Probability as a Fraction
- Probability as a Decimal and a Percentage
- Probability Summary

3. Determining Probabilities

- Types of Probability
- Calculating Probability
- Experimental Probability
- Using Simulations to Determine Probabilities
- Exploring Outcomes
- The Probability of Observations

Further Resources

- Unfortunate Events

A Chance of Rain

- A Chance of Rain
- A Chance of Rain Student Worksheet
- A Chance of Rain Teacher Guide

A Tree Snake Chance Game

- A Tree Snake Chance Game
- A Tree Snake Chance Game Student Worksheet
- A Tree Snake Chance Game Teacher Guide

Practice

- Mixed Practice: Finding Probability
- Practice: Experimental Probability
- Practice: Finding Probabilities

4. Complementary Events

- Complementary Events
- Calculating Complements

Practice

- Mixed Practice: Complementary Events
- Practice: Calculating Complements
- Practice: Complementary Events

5. Glossary

- Definitions List: Probability
- Definitions MCQ: Probability

6. Topic Tests

- Descriptions of Probability and Complementary Events
- Finding Probability
- Introduction to Probability


## Stage 5

## Financial mathematics

## A student

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01


## EP Lessons in 1. Financial mathematics A

## Outcome:

- solves financial problems involving simple interest, earning money and spending money MA5-FIN-C-01


## Content:

- Solve problems involving earning money
- Solve problems involving simple interest
- Solve problems involving spending money

1. Earning and Spending Money

- Salaries and Wages
- Commission
- Income Tax
- Piecework
- Royalties
- Timesheets
- Overtime, Special Rates and Allowances
- Goods and Sevices Tax

2. Simple Interest

- Introduction to Interest
- Calculating Simple Interest
- Rearranging the Simple Interest Formula


## EP Lessons in 2. Financial mathematics B

Outcome:

- solves financial problems involving compound interest and depreciation MA5-FIN-C-02


## Content:

- Solve problems involving compound interest and depreciation
- Compound Interest Basic Formula
- Rearranging the Compound Interest Formula
- Compound Interest - Months and Weeks
- Rearranging Compound Interest - Months and Weeks
- Mortgages
- Retirement
- Depreciation
- Definitions MCQ: Compound Interest
- Definitions MCQ: Financial Mathematics
- Definitions MCQ: Income, Tax and Simple Interest
- Spelling List: Financial Mathematics

3. Topic Test

- Compound Interest
- Definitions List: Compound Interest
- Definitions List: Financial Mathematics
- Definitions List: Income, Tax and Simple Interest


## Algebraic techniques

## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01


## EP Lessons in 1. Algebraic techniques A

## Outcome:

- simplifies algebraic fractions with numerical denominators and expands algebraic expressions MA5-ALG-C-01


## Content:

- Apply the 4 operations to simplify algebraic fractions with numerical denominators
- Apply the distributive law to the expansion of algebraic expressions, and collect like terms where appropriate


## EP Lessons in 2. Algebraic techniques B (Path)

## Outcome:

- $\quad$ simplifies algebraic fractions involving indices, and expands and factorises algebraic expressions (Path: Adv) MA5-ALG-P-01
Content:
- Apply the 4 operations involving algebraic fractions with pronumerals in the denominator
- Factorise algebraic expressions by taking out a common algebraic factor
- Expand binomial products and factorise monic quadratic expressions
- Variables, Conventions and Arithmetic
- Expanding Binomial Products
- Expanding and the Distributive Law
- Expanding Binomial Products II

Practice

- Practice: Expanding Binomial Products
- Practice: Expanding Binomial Products
- Identifying Algebraic Factors
- Identifying Complicated Algebraic Factors
- Simplifying Algebraic Fractions
- Adding Algebraic Fractions
- Subtracting Algebraic Fractions
- Multiplying Algebraic Fractions
- Dividing Algebraic Fractions
- Operations Including Binomial Fractions
- Factorising with Index Laws
- Factorisation by Grouping


## Practice

- Practice: Adding Algebraic Fractions
- Practice: Algebraic Fractions Extended
- Practice: Cancelling Common Factors
- Practice: Dividing Algebraic Fractions
- Practice: Factorisation by Grouping
- Practice: Factorising with Index Laws
- Practice: Multiplying Algebraic Fractions
- Practice: Subtracting Algebraic Fractions


## EP Lessons in 3. Algebraic techniques C (Path)

## Outcome:

- selects and applies appropriate algebraic techniques to operate with algebraic fractions, and expands, factorises and simplifies algebraic expressions (Path: Adv) MA5-ALG-P-02


## Content:

- Operate with algebraic fractions involving binomial numerators and numerical denominators
- Expand, factorise and simplify algebraic expressions including special products


## Additional resources

## 4. Glossary

- Definitions List: Algebraic Techniques
- Definitions MCQ: Algebraic Techniques
- Connecting Expanding and Factorising
- Expanding Cubic Expressions
- Expanding Perfect Squares
- Expanding Differences of Two Squares
- Factorising Quadratic Trinomials
- Factorising Perfect Squares
- Factorising Differences of Two Squares


## Practice

- Practice: Expanding to Trinomials
- Practice: Factorising Differences of Two Squares
- Practice: Factorising Perfect Squares
- Practice: Factorising Quadratic Trinomials
- Practice: Identifying Common Factors


## 5. Topic Test

- Algebraic Fractions


## Indices

## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01


## EP Lessons in 1. Indices A

## Outcome:

- simplifies algebraic expressions involving positive-integer and zero indices, and establishes the meaning of negative indices for numerical bases MA5-IND-C-01


## Content:

- Extend and apply the index laws to variables using positive-integer indices and the zero index
- Simplify algebraic products and quotients using index laws
- Apply index laws to numerical expressions with negative-integer indices
- Multiplying Powers
- Dividing Powers
- The Zero Index
- Powers as the Base of Another Power
- Multiplication as the Base of a Power
- Division as the Base of a Power
- Simplifying Algebraic Products with Index Laws
- Simplifying Algebraic Quotients with Index Laws

Practice

- Practice: Dividing Powers
- Practice: Division as the Base of a Power
- Practice: Integers
- Practice: Multiplication as the Base of a Power
- Practice: Multiplying Powers
- Practice: Positive Integer Indices
- Practice: Powers as the Base of Another Power
- Practice: The Zero Index


## EP Lessons in 2. Indices B (Path)

## Outcome:

- applies the index laws to operate with
algebraic expressions involving negative-integer indices (Path: Adv) MA5-IND-P-01


## Content:

- Apply index laws to algebraic expressions involving negative-integer indices
- Applying Index Laws
- Positive and Negative Integer Indices

Practice

- Practice: Applying Index Laws
- Practice: Negative Integer Indices


## EP Lessons in 3. Indices C (Path)

## Outcome:

- describes and performs operations with surds and fractional indices (Path: Adv) MA5-IND-P-02


## Content:

- Describe surds
- Apply knowledge of surds to solve problems
- Describe and use fractional indices
- The Real Number System
- Exact Values and Approximate Values
- Fractional Indices
- Introduction to Surds
- Index Laws and Fractional Powers
- Simplifying Surds
- Adding and Subtracting Surds
- Multiplying and Dividing Surds
- Expanding Surds
- Rationalising Denominators
- Applications of Surds
- Conjugate and Perfect Square Surds Pracitce
- Practice: Fractional Indices


## Additional resources

## 4. Glossary

- Definitions List: Indices
- Definitions MCQ: Indices
- Spelling List: Indices

5. Topic Test

- Simplifying Algebraic Products and Integer Indices


## Equations

## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01


## EP Lessons in 1. Equations A

## Outcome:

- solves monic quadratic equations, linear inequalities and cubic equations of the form
『ax』^3=k (Path: Adv) MA5-EQU-P-01


## Content:

- Solve linear equations involving up to 3 steps
- Solve linear equations involving one algebraic fraction
- Solve linear equations arising from word problems and substitution into formulas
- Word Problems
- Rearranging and Solving Equations
- Solving Word Problems
- Solving Using Algebraic Methods
- Non-Integer Solutions to Linear Equations
- Applications of Linear Equations Practice
- Practice: Rearranging and Solving Equations
- Practice: Solving Word Problems
- Practice: Word Problems
- Introduction to Inequalities
- Investigating Linear Inequalities with

Technology

- Solving Inequalities
- Rearranging Inequalities
- Chained Inequalities
- Review Lesson: Inequalities
- Monic Factorisation
- Solving Monic Quadratic Equations Practice
- Practice: Chained Inequalities


## EP Lessons in 3. Equations C (Path)

## Outcome

- solves linear equations of more than 3 steps, monic and non-monic quadratic equations, and linear simultaneous equations ( $P$ ath: Adv) MA5-EQU-P-02


## Content:

- Solve linear equations involving algebraic fractions and equations of more than 3 steps
- Rearrange literal equations
- Solve quadratic equations using a variety of methods
- Solve linear simultaneous equations, both algebraically and graphically


## 1. Solve Quadratic Equations

- Factorising Quadratic Expressions
- Solving Quadratic Equations Using Technology
- Guess and Check
- The Quadratic Formula
- Using the Quadratic Formula
- Completing the Square: Method 1- Using Rearrangement
- Completing the Square: Method 2 - Using Differences of Two Squares
- Grouping
- Factorising by Completing the Square
- Non-Monic Factorisation
- Solving Non-Monic Quadratic Equations

Practice

- Practice: Completing the Square
- Practice: Completing the Square Using Differences of Two Squares
- Practice: Factorising Quadratic Expressions
- Practice: Factorising by Completing the Square
- Practice: Grouping
- Practice: Guess and Check
- Practice: Solving Quadratic Equations Using Technology
- Practice: The Quadratic Formula


## 2. Solve Linear Simultaneous Equations

- Using Graphs to Solve Simultaneous Equations
- Using Elimination to Solve Simultaneous Equations
- Using Substitution to Solve Simultaneous Equations
Practice
- Practice: Using Elimination to Solve Simultaneous Equations
- Practice: Using Graphs to Solve Simultaneous Equations
- Practice: Using Substituation to Solve Simultaneous Equations


## Additional resources

## 4. Glossary

- Definitions List: Equations
- Definitions MCQ: Equations


## 5. Topic Test

- Solving Quadratic Equations


## Linear relationships

## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01


## EP Lessons in 1. Linear relationships A

## Outcome:

- determines the midpoint, gradient and length of an interval, and graphs linear relationships, with and without digital tools MA5-LIN-C-01


## Content:

- Find the midpoint and gradient of a line segment (interval) on the Cartesian plane
- Find the distance between 2 points located on the Cartesian plane
- Recognise and graph equations
- Examine parallel, horizontal and vertical lines


## EP Lessons in 2. Linear Relationships B

## Outcome:

- graphs and interprets linear relationships using the gradient/slope-intercept form MA5-LIN-C-02


## Content:

- Examine the gradient/slope-intercept form
- Find the equations of parallel and perpendicular lines

1. Find the Midpoint and Gradient

- Line Segments on Cartesian Planes
- Distance and Pythagoras' Theorem
- Gradient of a Line Segment
- Midpoint of a Line Segment
- Applications of Coordinate Geometry: Distance
- Applications of Coordinate Geometry: Midpoint

Practice

- Practice: Calculating the Gradient
- Practice: Distance and Pythagoras' Theorem
- Practice: Identifying Coordinates
- Practice: Line Segments on Cartesian Planes
- Practice: Midpoint of a Line Segment
- Drawing Linear Graphs Using the Gradient
- Applications of Coordinate Geometry: Gradient
- Parallel Lines
- Perpendicular Lines

Practice

- Practice: Drawing Linear Graphs Using the Gradient
- Practice: Parallel Lines
- Practice: Perpendicular Lines

2. Recognise and Graph Equations

- Plotting Linear Graphs
- Graphing Using Technology - Casio Calculators
- Practice
- Practice: Plotting Linear Graphs

3. Horizontal, Parallel and Perpendicular Lines

- Horizontal and Vertical Lines
- Parallel Lines
- Perpendicular Lines

Practice

- Practice: Horizontal and Vertical Lines
- Practice: Parallel Lines
- Practice: Perpendicular Lines


## EP Lessons in 3. Linear Relationships C (Path)

## Outcome:

- describes and applies transformations, the midpoint, gradient/slope and distance formulas, and equations of lines to solve problems (Path: Adv) MA5-LIN-P-01


## Content:

- Apply formulas to find the midpoint and gradient/slope of an interval on the Cartesian plane
- Apply the distance formula to find the distance between 2 points located on the Cartesian plane
- Use various forms of the equation of a straight line
- Solve problems by applying coordinate geometry formulas
- Identify line and rotational symmetries
- Describe translations, reflections in an axis, and rotations through multiples of 90 degrees on the Cartesian plane, using coordinates
- Line Segments on Cartesian Planes
- Distance and Pythagoras' Theorem
- Gradient of a Line Segment
- Midpoint of a Line Segment
- Applications of Coordinate Geometry: Distance
- Applications of Coordinate Geometry: Gradient
- Applications of Coordinate Geometry: Midpoint
- Translation
- Reflection
- Rotation

Practice

- Mixed Practice: Transformations
- Practice: Distance and Pythagoras' Theorem
- Practice: Gradient of a Line Segment
- Practice: Line Segments on Cartesian Planes
- Practice: Midpoint of a Line Segment
- Practice: Reflection
- Practice: Rotation
- Practice: Translation


## Additional resources

4. Glossary

- Definitions List: Linear Relationships
- Definitions MCQ: Linear Relationships

5. Topic Test

- Linear Relationships


## Non-linear relationships

## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01


## EP Lessons in 1. Non-linear relationships A

## Outcome:

- identifies connections between algebraic and graphical representations of quadratic and exponential relationships in various contexts MA5-NLI-C-01


## Content:

- Examine the connection between algebraic and graphical representations of quadratics and exponentials
- Linear and Non-Linear Relationships
- Parabolas
- Exponential Graphs


## EP Lessons in 2. Non-linear relationships B

## Outcome:

- identifies and compares features of parabolas and exponential curves in various contexts MA5-NLI-C-02


## Content:

- Graph and examine quadratic relationships
- Graph and examine exponential relationships
- Distinguish between linear, quadratic and exponential relationships by examining their graphical representations
- Features of Polynomial Graphs
- Features of Graphs - Roots


## EP Lessons in 3. Non-linear relationships C (Path)

## Outcome:

- interprets and compares non-linear relationships and their transformations, both algebraically and graphically (Path: Adv) MA5-NLI-P-01


## Content:

- Graph parabolas and describe their features and transformations
- Graph exponentials and describe their features and transformations
- Graph hyperbolas and describe their features and transformations
- Graph circles and describe their features and transformations
- Distinguish between different types of graphs by examining their algebraic and graphical representations and solve problems
- Graph and compare polynomial curves and describe their features and transformations

1. Non-Linear Graphs

- Transforming Parabolas - Translation
- Transforming Parabolas - Dilation and Reflection
- Circle Graphs
- Transforming Circles
- Exponential Graphs I
- Exponential Graphs II
- Hyperbola Graphs
- Hyperbola Graph Transformations

Practice

- Practice: Exponential Graphs
- Practice: Transforming Circles
- Practice: Transforming Parabolas - Dilation and Reflection
- Practice: Transforming Parabolas - Translation


## 2. Polynomial Graphs

- Parabolas
- Parabola Transformations
- Multiple Transformations of Parabolas
- Cubics
- Cubic Transformations
- Quartics


## Additional resources

## 4. Spelling and Definitions

- Definitions List: Non-Linear Relationships
- Definitions MCQ: Non-Linear Relationships


## 5. Topic Test

- Non-Linear Relationships


## Numbers of any magnitude

## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01


## EP Lessons in 7. Numbers of any magnitude

## Outcome:

- solves measurement problems by using scientific notation to represent numbers and rounding to a given number of significant figures MA5-MAG-C-01
Content:
- Identify and describe very small and very large measurements
- Find absolute and percentage error
- Estimate and round numbers to a specified degree of accuracy
- Express numbers in scientific notation
- Rounding to Significant Figures
- Rounding Sensibly
- Leading Digit Approximation
- Precision and Accuracy
- Precision in Context
- Absolute vs. Relative Error
- Limits of Accuracy
- Introduction to Scientific Notation (Standard Form) - Large Numbers
- Introduction to Scientific Notation (Standard Form) - Small Numbers
- Ordering Numbers and Estimating Calculations in Scientific Notation (Standard Form)
- Adding and Subtracting with Scientific Notation (Standard Form)
- Multiplying and Dividing in Scientific Notation (Standard Form)
- Significant Figures and Scientific Notation (Standard Form)
- Time Scales
- Representing Very Large and Very Small Units

Glossary

- Definitions List: Numbers of Any Magnitude
- Definitions MCO: Numbers of Any Magnitude

Topic Test

- Numbers of Any Magnitude


## Pythagoras and trigonometry

## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01


## EP Lessons in 1. Trigonometry A

## Outcome:

- applies trigonometric ratios to solve right-angled triangle problems MA5-TRG-C-01
Content:
- Demonstrate and explain the constancy of trigonometric ratios for a given angle in right-angled triangles
- Apply trigonometry to solve right-angled triangle problems


## EP Lessons in 2. Trigonometry B

## Outcome:

- applies trigonometry to solve problems, including bearings and angles of elevation and depression MA5-TRG-C-02


## Content:

- Solve right-angled triangle problems involving angles of elevation and depression
- Solve right-angled triangle problems involving bearings
- Introduction to Trigonometry
- Finding Side Lengths Using Trigonometry
- Finding Angles Using Trigonometry
- Review Lesson: Trigonometric Ratios
- Angles of Elevation and Depression
- Bearings with Right-Angled Triangles
- Using Trigonometric Functions in Real World Applications
- Using_Inverse Trigonometric Functions in Real World Applications
- Applications of Trigonometry in Coding


## EP Lessons in 3. Trigonometry C (Path)

## Outcome:

- uses function notation to describe and graph functions of one variable and graphs inequalities in one and 2 variables (Path: Adv) MA5-FNC-P-01


## Content:

- Solve 3-dimensional problems involving right-angled triangles
- Apply the sine, cosine and area rules to any triangle and solve related problems


## EP Lessons in 4. Trigonometry D (Path)

## Outcome:

- establishes and applies the properties of trigonometric functions and finds solutions to trigonometric equations (Path: Adv) MA5-TRG-P-02


## Content:

- Use the unit circle to define trigonometric functions and represent them graphically
- Solve trigonometric equations using exact values and the relationships between supplementary and complementary angles


## 1. Trigonometric Rules

- The Sine Rule
- Finding Angles Using the Sine Rule
- The Sine Rule: The Ambiguous Case
- The Cosine Rule
- Finding Angles Using the Cosine Rule
- Pythagorean Triples
- Review Lesson: Trigonometric Rules

2. Area of a Triangle

- Area of a Triangle: $\geqslant \gg a b \sin C$
- Heron's Formula

3. Pythagoras' Theorem and Trigonometry in 3D

- Pythagoras' Theorem in 3D
- Trigonometry in 3D
- 3D Problems Using Right-Angled Triangles

Extended Investigations

- Building with Pythagoras
- Pirates' Treasure
- Airplane Flight Paths
- Bearings with Right-Angled Triangles

1. Defining and Graphing Trigonometric Functions

- The Unit Circle and Radians
- Understanding and Graphing Sine
- Understanding and Graphing Cosine
- Understanding and Graphing Tangent
- Comparing Trigonometric Functions

2. Solving Simple Trigonometric Equations

- Special Triangles: 30-60-90
- Special Triangles: 45-45-90
- Trigonometric Ratios and Complementary Angles
- Balloons Over Waikato
- Forestry Subdivision


## Additional resources

## 5. Glossary

- Definitions List: Right-Angled Triangles (Trigonometry)
- Definitions MCQ: Right-Angled Triangles (Trigonometry)
- Spelling List: Pythagoras and Trigonometry


## 6. Topic Tests

- Inverse Trig, Bearings and Elevation
- Right-Angle Triangles


## Area and surface area

## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01


## EP Lessons in 1. Area and surface area A

## Outcome:

- solves problems involving the surface area of right prisms and practical problems involving the area of composite shapes and solids MA5-ARE-C-01


## Content:

- Solve problems involving areas and surface areas
- Develop and apply the formula for surface areas of cylinders
- Solve problems involving surface areas of cylinders and related composite solids

1. Area

- Area of Composite Shapes I
- Area of Composite Shapes II
- Area of Rectangles \& Squares
- Area of Triangles
- Area of Parallelograms
- Area of Rhombuses and Kites
- Area of Trapeziums

Practice

- Practice: Area of Composite Shapes

2. Surface Area

- Surface Area of Prisms
- Surface Area of Cylinders
- Surface Area of Complex Solids
- Composite Shapes and Solids
- Surface Area of Composite Solids

Practice

- Mixed Practice: Surface Area
- Practice: Surface Area
- Practice: Surface Area of Complex Solids
- Practice: Surface Area of Cylinders
- Practice: Surface Area of Prisms

EP Lessons in 2. Area and surface area B

## Outcome:

- applies knowledge of the surface area of right pyramids and cones, spheres and composite solids to solve problems (Path: Stn, Adv) MA5-ARE-P-01


## Content:

- Solve problems involving surface areas


## Additional resources

## 3. Glossary

- Definitions List: Area and Surface Area
- Definitions MCQ: Area and Surface Area


## 4. Topic Tests

- Area and Surface Area
- Surface Area


## Volume

## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01


## EP Lessons in 1. Volume A

## Outcome:

- solves problems involving the volume of composite solids consisting of right prisms and cylinders MA5-VOL-C-01
Content:
- Solve problems involving composite solids consisting of right prisms and cylinders


## EP Lessons in 2. Volume B

## Outcome:

- applies knowledge of the volume of right pyramids, cones and spheres to solve problems involving related composite solids (Path: Stn, Adv) MA5-VOL-P-01


## Content:

- Solve problems involving volumes
- Volume of Rectangular Prisms
- Calculating Volume of Triangular Prisms
- Calculating Volume of Cylinders
- Calculating Volume of Other Regular and Irregular Prisms
- Volume of Composite Solids


## Practice

- Mixed Practice: Volume
- Practice: Volume
- Practice: Volume of Composite Solids


## Additional resources

## 3. Glossary

- Definitions List: Volume
- Definitions MCQ: Volume
- Volume of Right Pyramids
- Volume of Right Cones
- Volume of Spheres
- Volume of Composite Solids


## 4. Topic Test

- Calculating Volume


## Properties of geometrical figures

## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01


## EP Lessons in 1. Properties of geometrical figures $\mathbf{A}$

## Outcome:

- identifies and applies the properties of similar figures and scale drawings to solve problems MA5-GEO-C-01


## Content:

- Identify and describe the properties of similar figures
- Solve problems using ratio and scale factors in similar figures
- The Enlargement Transformation
- Introduction to Scaling
- Magnitude
- Magnitude as a Ratio
- Scaling on Cartesian Planes


## Practice

- Practice: Introduction to Scaling
- Practice: Introduction to Similarity
- Practice: Magnitude
- Practice: Magnitude as a Ratio
- Practice: Scaling on Cartesian Planes


## EP Lessons in 2. Properties of geometrical figures B (Path)

## Outcome:

- establishes conditions for congruent triangles and similar triangles and solves problems relating to properties of similar figures and plane shapes (Path: Ext) MA5-GEO-P-01


## Content:

- Identify and explain congruence
- Develop and use the conditions for congruent triangles
- Develop and apply the minimum conditions for triangles to be similar
- Establish and apply properties of similar shapes and solids
- Apply logical reasoning to numerical problems involving plane shapes

1. Congruence

- Introduction to Congruence
- Conditions for Congruence: SSS and SAS
- Conditions for Congruence: ASA, AAS and HL
- Working with Congruent Triangles
- Congruence of Squares, Rectangles and Parallelograms
- Congruence of Rhombuses, Trapeziums and Kites
Practice
- Practice: ASA, AAS and HL Congruence Tests
- Practice: Congruence of Rhombuses, Trapeziums and Kites
- Practice: Congruence of Squares, Rectangles and Parallelograms
- Practice: SSS and SAS Congruence Tests
- Practice: Triangles
- Practice: Working with Congruent Triangles


## 2. Similarity

- Introduction to Similarity
- Similarity Tests
- Similarity and Angles
- Creating Algorithms and Flowcharts

3. Plane shapes

- Rotation and Reflection of Plane Shapes
- Translation and Congruence of Plane Shapes
- Polygons and Interior Angles
- Polygons and Exterior Angles

Practice

- Practice: Reflection
- Practice: Rotation
- Practice: Rotation and Reflection of Plane Shapes
- Practice: Symmetry
- Practice: Translation
- Practice: Translation and Congruence of Plane Shapes


## EP Lessons in 3. Properties of geometrical figures C (Path)

## Outcome:

- constructs proofs involving congruent triangles and similar triangles and proves properties of plane shapes (Path: Ext) MA5-GEO-P-02


## Content:

- Construct formal proofs involving congruent and similar triangles
- Apply logical reasoning to proofs involving plane shapes


## Additional resources

## 4. Glossary

- Definitions List: Geometric Reasoning
- Definitions List: Geometry
- Definitions MCQ: Geometric Reasoning
- Definitions MCQ: Geometry
- Introduction to Proofs and Logic
- Angle Proofs
- Parallelogram and Rhombus Proofs
- Rectangle and Square Proofs
- Applications of Geometric Reasoning Practice
- Practice: Angle Proofs
- Practice: Applications of Geometric Reasoning
- Practice: Introduction to Proofs and Logic
- Practice: Parallelogram and Rhombus Proofs
- Practice: Rectangle and Square Proofs

5. Topic Tests

- Angles
- Proofs


## Data analysis

## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01


## EP Lessons in 1. Data analysis A

## Outcome:

- compares and analyses datasets using summary statistics and graphical representations MA5-DAT-C-01


## Content:

- Examine standard deviation as a measure of spread
- Determine quartiles and interquartile range
- Represent datasets using box plots and use them to compare datasets
. Standard deviation as a measure of spread
- Mean and Standard Deviation
- Calculating Standard Deviation
- Calculating Standard Deviation Using Technology
- Investigating the Standard Deviation
- Measures of Centre in Grouped Data
- Comparing the Measures of Spread
- Finding Measures of Centre and Spread

Practice

- Practice: Measures of Centre in Grouped Data

2. Determine quartiles and interquartile range

- Introduction to Box and Whisker Plots
- Range
- Quartiles and Interquartile Range
- Five Point Summary

Practice

- Practice: Five Point Summary
- Practice: Interquartile Range
- Practice: Quartiles
- Practice: Range

3. Representing and comparing data

- Comparing Data Sets
- Back-to-Back Stem and Leaf Plots
- Comparing Dot Plots
- Comparing Histograms
- Using the Standard Deviation to Compare Data Sets
- Building Box and Whisker Plots
- Comparing Box and Whisker Plots
- Box and Whisker Plots. Histograms and Dot Plots

Practice

- Mixed Practice: Comparing Data
- Practice: Back-to-Back Stem and Leaf Plots
- Practice: Comparing Data Sets
- Practice: Comparing Dot Plots
- Practice: Comparing Histograms


## EP Lessons in 2. Data analysis B

## Outcome:

- displays and interprets datasets involving bivariate data MA5-DAT-C-02
Content:
- Identify and describe numerical datasets involving 2 variables
- Represent datasets involving 2 numerical variables, using a scatter plot and a line of best fit, by eye
- Interpret data involving 2 numerical variables, using graphical representations


## 1. Bivariate data

- Introduction to Bivariate Data
- Bivariate Variables
- Plotting Using a Calculator
- Plotting Using a Spreadsheet
- Analysing Trend by Eye
- Cleaning Bivariate Data
- Introduction to Time Series
- Analysing Time Series


## 2. Lines of best fit

- Lines of Best Fit by Eye
- Least Squares Fitting using a Calculator
- Least Squares Fitting using a Spreadsheet
- Making Predictions by Eye
- Making Predictions Using the Equation
- Testing Regression Models Using A Calculator
- Testing Regression Models Using A Spreadsheet


## EP Lessons in 3. Data analysis C

## Outcome:

- plans, conducts and reviews a statistical inquiry into a question of interest (Path: Stn, Adv) MA5-DAT-P-01


## Content:

- Plan and conduct a statistical inquiry into a question of interest
- Examine reports of studies in digital media and elsewhere for information on their planning and implementation

1. Plan and conduct a statistical inquiry

- What is Sampling?
- Types of Sampling: Probability Sampling
- Types of Sampling: Non-Probability Sampling
- Sampling Errors

2. Examine reports

- Statistical Reports In The Media
- Public Opinion Surveys
- Cultural Bias
- Analysing Sampling in Reports
- Misleading Reports
- Statistics in Organisation


## Additional resources

## 4. Glossary

- Definitions List: Bivariate Data Analysis
- Definitions List: Data Representation and Interpretation
- Definitions List: Single Variable Data Analysis
- Definitions MCQ: Bivariate Data Analysis

Definitions MCQ: Single Variable Data Analysis

- Spelling List: Data Representation and Interpretation
- Spelling List: Data Representation and Interpretation


## 5. Topic Tests

- Analysing and Comparing Data
- Bivariate Data Analysis
- Data Sources and Statistical Reports
- Lines of Best Fit


## Probability

## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01


## EP Lessons in 1. Probability A

## Outcome

- solves problems involving probabilities in multistage chance experiments and simulations MA5-PRO-C-01


## Content:

- Describe multistage chance experiments involving independent and dependent events
- Solve problems for multistage chance experiments
- Design and use simulations to model and examine situations involving probability


## 1. Independence

- Introduction to Independence
- Investigating Independent Events using Chance Diagrams
- Independent and Dependent Events

Practice

- Practice: Introduction to Independence
- Practice: Investigating Independent Events using Chance Diagrams

2. Two-step experiments

- Introduction to Two-Step Experiments
- Tree Diagrams
- Using Tree Diagrams
- Arrays
- Using Arrays
- Unfortunate Events

Practice

- Practice: Arrays
- Practice: Introduction to Two-Step Chance
- Practice: The Probability Adventure
- Practice: Tree Diagrams
- Practice: Using Arrays
- Practice: Using Tree Diagrams

3. Multi-step events

- Arrays
- Probabilities and Three-Step Experiments
- Building Three-Step Tree Diagrams
- Tree Diagrams with Unequal Outcomes
- Probabilities of Unequal Outcomes
- Three-Step Experiments and Unequal Outcomes


## Practice

- Practice: Arrays
- Practice: Building Three-Step Tree Diagrams
- Practice: Probabilities and Three-Step Experiments
- Practice: Probabilities of Unequal Outcomes
- Practice: Three-Step Experiments and Unequal Outcomes
- Practice: Tree Diagrams with Unequal Outcomes

4. Using simulations to model probability

- Using Simulations to Compare Probabilities
- Simulating Traditional Indigenous Games


## EP Lessons in 2. Probability B (Path)

## Outcome:

- solves problems involving Venn diagrams, 2-way tables and conditional probability (Path: Adv) MA5-PRO-P-01
Content:
- Solve problems involving Venn diagrams and 2-way tables
- Use the language, 'if ... then', 'given', 'of' and 'knowing that', to examine conditional statements and identify common mistakes in interpreting the language
- Describe mutually and non-mutually exclusive events using specific language and calculate related probabilities
- Introduction to Conditional Probability
- Investigating Conditional Probability with Venn Diagrams
- Investigating Conditional Probability with Two-Way Tables
- Calculating Conditional Probability Using Tree Diagrams
- Calculating Conditional Probabilities using Arrays
- Word Problems

Practice

- Practice: Calculating Conditional Probabilities Using Arrays
- Practice: Calculating Conditional Probability Using Tree Diagrams
- Practice: Introduction to Conditional Probability
- Practice: Investigating Conditional Probability with Two-Way Tables
- Practice: Investigating Conditional Probability with Venn Diagrams
- Practice: Word Problems
- Conditional Probability
- Venn Diagrams and Two-Way Tables


## Ratios and rates

## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01


## EP Lessons in 1. Variation and rates of change A (Path)

## Outcome:

- identifies and solves problems involving direct and inverse variation and their graphical representations (Path: Stn, Adv) MA5-RAT-P-01


## Content:

- Identify and describe problems involving direct and inverse variation
- Identify and describe graphs involving direct and inverse variation
- Solve problems involving direct and inverse variation and examine the relationship between graphs and equations corresponding to proportionality
- Rates
- Direct Proportion
- Introduction to Inverse Proportion
- Applying Inverse Proportion
- Introduction to Graphs

Practice

- Practice: Applying Inverse Proportion
- Practice: Direct Proportion
- Practice: Introduction to Graphs
- Practice: Introduction to Inverse Proportion


## EP Lessons in 2. Variation and rates of change B (Path)

## Outcome:

- analyses and constructs graphs relating to rates of change (Path: Adv) MA5-RAT-P-02
Content:
- Analyse graphs that are decreasing or increasing at a constant rate
- Analyse the relationship between graphs and variable rates of change
- Construct graphical representations of rates of change
- Constant Rates
- Reading Constant Rates
- Drawing Constant Rates
- Variable Rates
- Rates of Change
- Analysing Rates of Change
- Analysing Graphs


## Practice

- Practice: Analysing Graphs
- Practice: Constant Rates
- Practice: Rates of Change
- Practice: Variable Rates


## Additional resources

- Definitions List: Ratios and Rates
- Definitions MCQ: Ratios and Rates


## Polynomials (Path)

## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01


## EP Lessons in 15. Polynomials (Path)

## Outcome:

- defines, operates with and graphs polynomials and applies the factor and remainder theorems to solve problems (Path: Adv, Ext) MA5-POL-P-01
Content:
- Define and operate with polynomials
- Divide polynomials
- Apply the factor and remainder theorems to solve problems
- Graph polynomials
- Introduction to Polynomials
- Evaluating Polynomials
- Adding, Subtracting and Multiplying Polynomials
- Dividing Polynomials
- The Remainder Theorem
- The Factor Theorem
- Factorising Quartic Polynomials
- Solving Polynomials
- Fractal Trees and Recursion (Year 7-10)
- Patterns Found in Nature (Year 5-10)

Practice

- Practice: Adding, Subtracting and Multiplying Polynomials
- Practice: Dividing Polynomials
- Practice: Evaluating Polynomials
- Practice: Factorising Cubic Polynomials
- Practice: Factorising Quartic Polynomials
- Practice: Introduction to Polynomials
- Practice: Solving Polynomials
- Practice: The Factor Theorem
- Practice: The Remainder Theorem


## Glossary

- Definitions List: Polynomials
- Definitions MCQ: Polynomials
- Spelling List: Polynomials

Topic Test

- Topic Test: Polynomials


## Logarithms (Path)

## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01


## EP Lessons in 16. Logarithms (Path)

## Outcome:

- establishes and applies the laws of logarithms to solve problems (Path: Adv) MA5-LOG-P-01
Content:
- Examine logarithms both numerically and graphically
- Establish and apply the laws of logarithms to solve problems
- Introduction to Logarithms
- Deriving the Laws of Logarithms
- Using the Laws of Logarithms
- Combining Log Laws
- Logarithmic Scales
- Solving Exponential Equations


## Functions and other graphs (Path)

## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01


## EP Lessons in 17. Functions and other graphs (Path)

## Outcome:

- uses function notation to describe and graph functions of one variable and graphs inequalities in one and 2 variables (Path: Adv) MA5-FNC-P-01


## Content:

- Define relations and functions, and use function notation
- Find the domain and range of a function and graph functions
- Graph regions corresponding to linear inequalities in one and 2 variables
- Introduction to Functions
- Function Notation
- Inverse Functions and Transformations


## Circle geometry (Path)

## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01


## EP Lessons in 18. Circle geometry (Path)

## Outcome:

- applies deductive reasoning to prove circle theorems and solve related problems (Path: Ext) MA5-CIR-P-01
Content:
- Prove and apply angle and chord properties of circles
- Prove and apply tangent and secant properties of circles

1. Angle theorems for circles

- Central Angle Theorem
- Proof: Central Angle Theorem
- Angles Subtended by the Same Arc
- Thales' Theorem: Angles in a Semicircle
- Proving Thales' Theorem
- Cyclic Quadrilaterals

2. Chord properties

- Equal Length Chord Properties
- Perpendicular Bisector to Chords
- Tangents, Secants and the Alternate Segment Theorem
- Intersecting Chords, Secants and Tangents


## 3. Glossary

- Definitions List: Circle Geometry
- Definitions MCQ: Circle Geometry
- Spelling List: Circle Geometry


## Introduction to networks (Path)

## A student:

- develops understanding and fluency in mathematics through exploring and connecting mathematical concepts, choosing and applying mathematical techniques to solve problems, and communicating their thinking and reasoning coherently and clearly MAO-WM-01


## EP Lessons in 19. Introduction to networks (Path)

## Outcome:

- solves problems involving the characteristics of graphs/networks, planar graphs and Eulerian trails and circuits (Path: Stn) MA5-NET-P-01
Content:
- Examine and describe a graph/network
- Define a planar graph and apply Euler's formula for planar graphs
- Explain the concept of Eulerian trails and circuits in the context of the Königsberg bridges problem
- Understanding Graph Terminology and Representing Practical Situations Using Networks
- Equivalent Networks
- Euler's Formula and Polyhedra
- The Seven Bridges of Königsberg
- Network Diagrams

